

# MINITAB tutorial TA session

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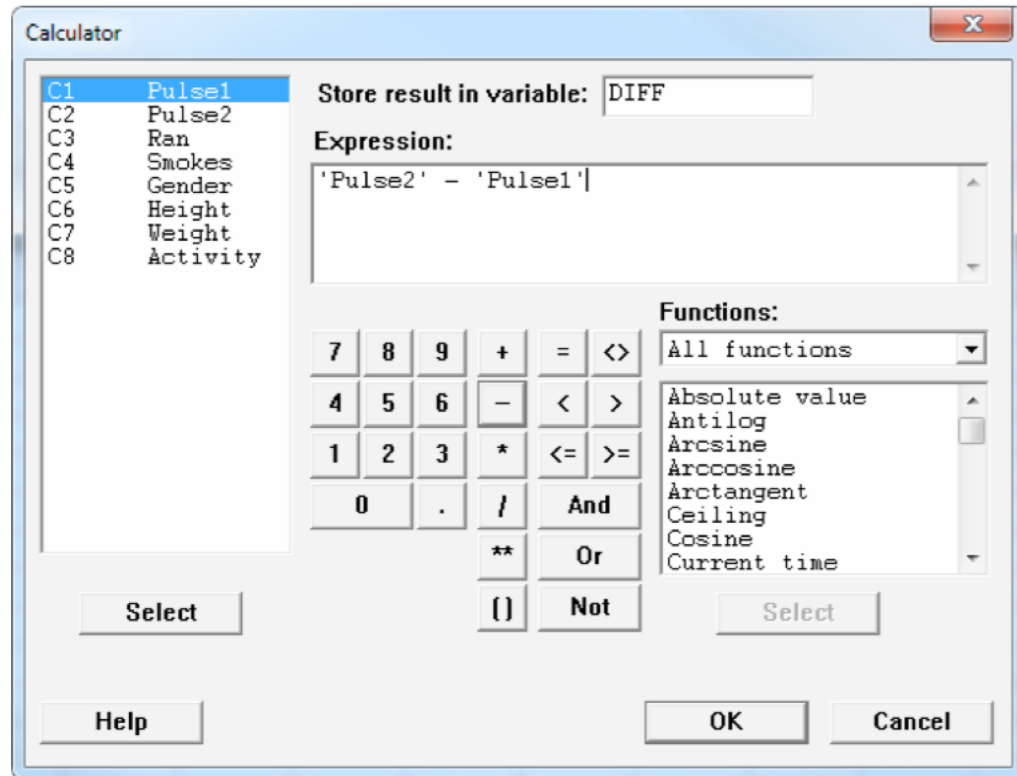
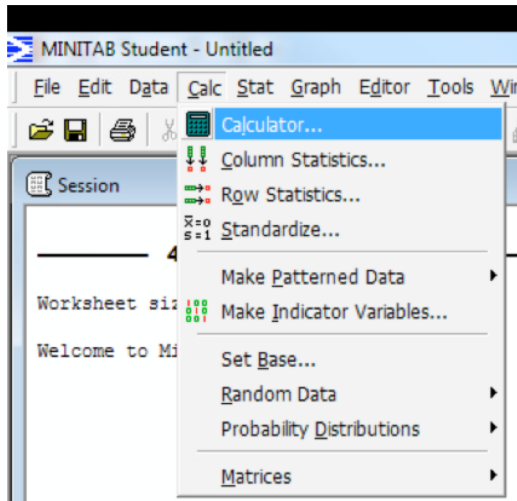
# Table of contents

- Calculator, basic statistics, histogram, boxplot, percentile in a column of data
- Probability distribution,
- Random data, row statistics, column statistics, monte carlo, bootstrap
- T-test, z test, power analysis, probability plot
- Control charts
- Scatter plot, regression



# Calculator

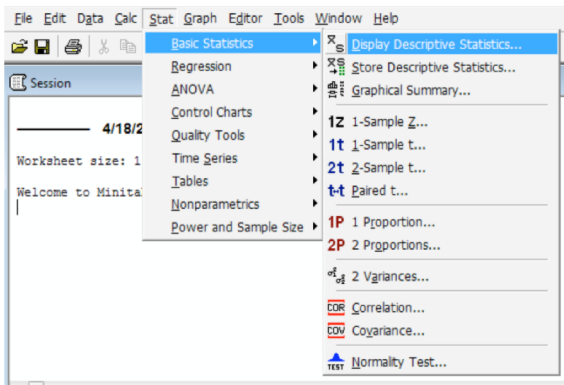
Calc->Calculator



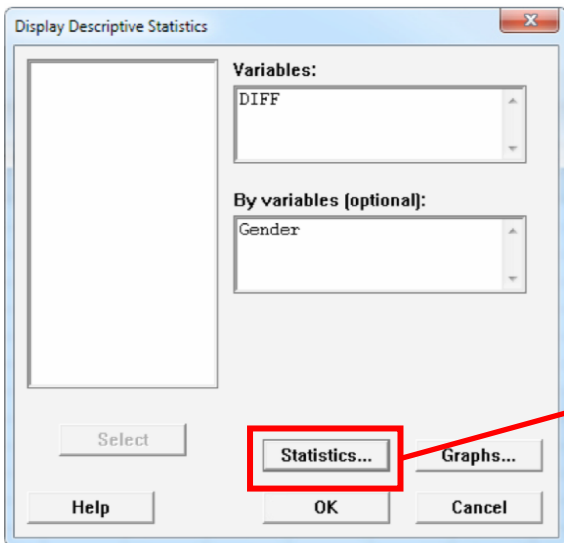


# Basic statistics

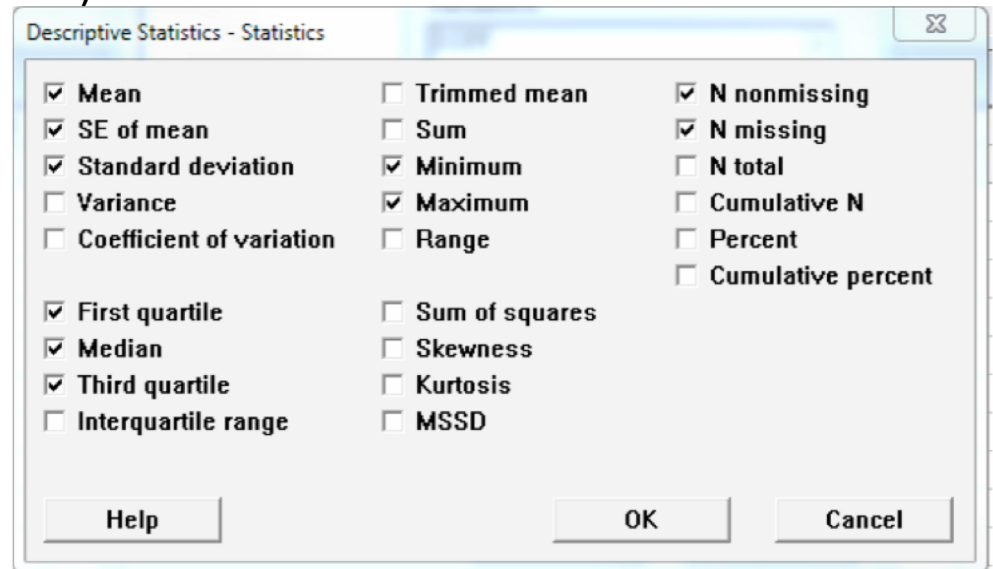
1. Stat->Basic Statistics->Display Descriptive Statistics



2. Input variables and By variables(optional)



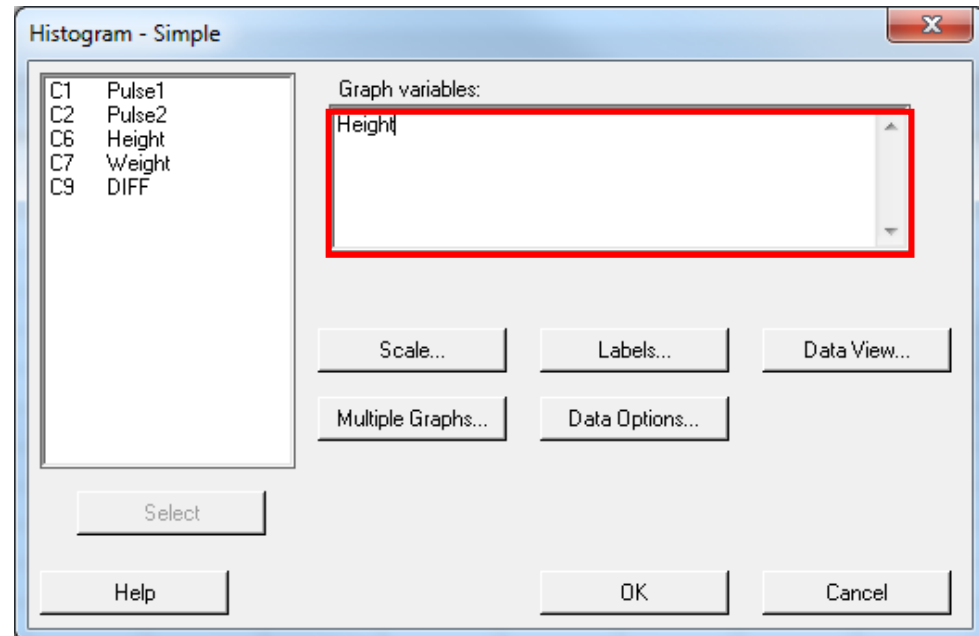
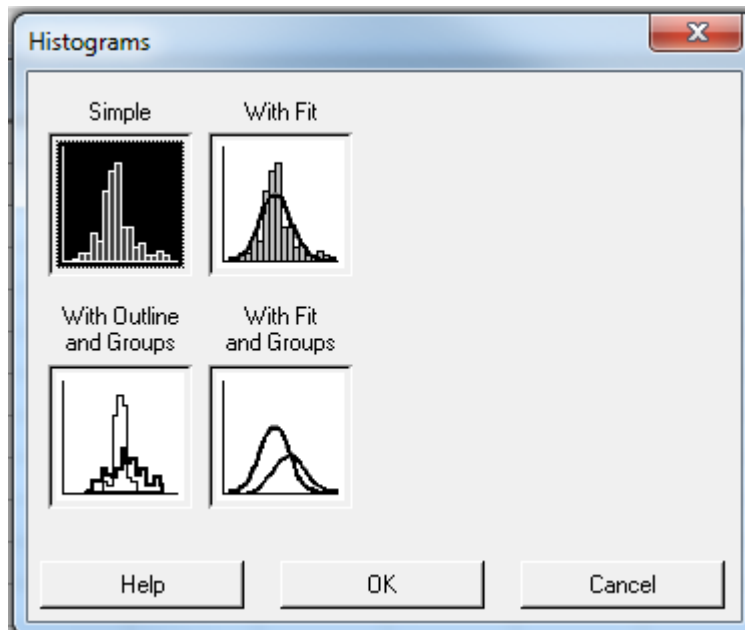
3. In Statistics, we can choose information we want



# Histogram

- Graph-> Histogram

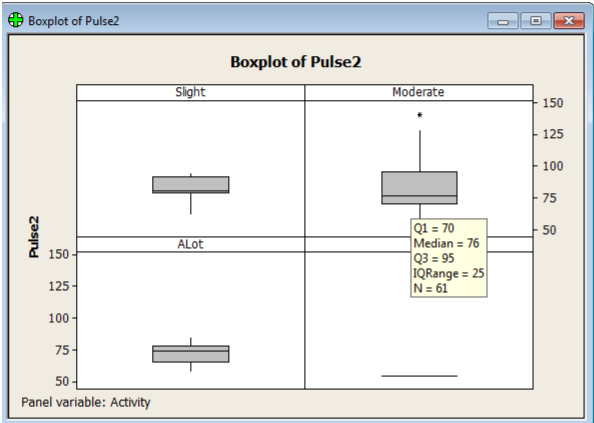
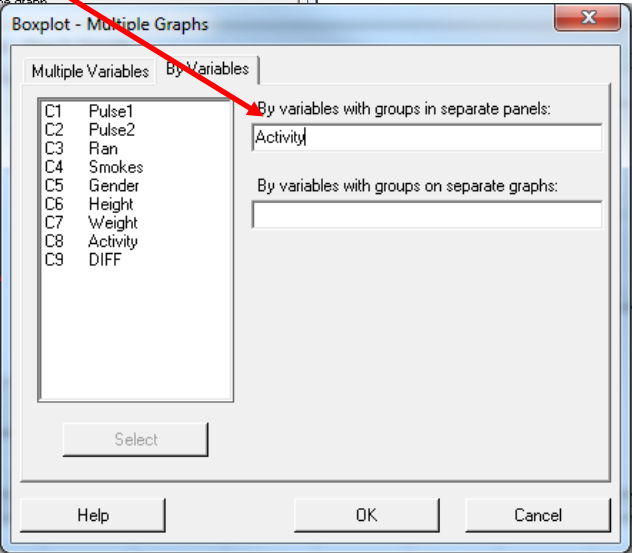
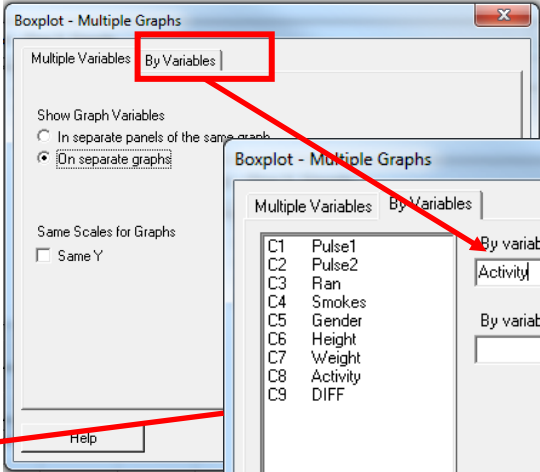
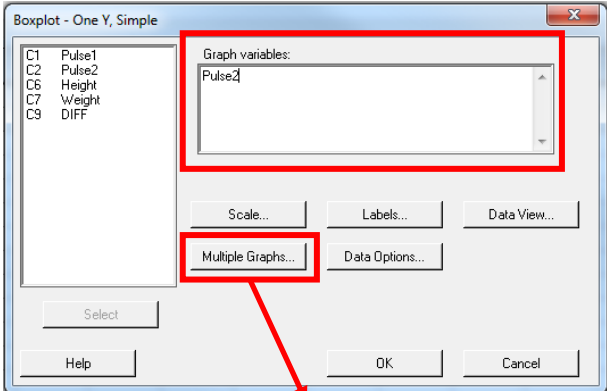
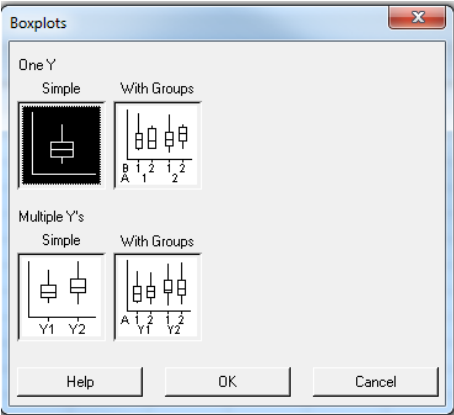
Input the variable



Obtain side-by-side boxplot of Pulse2 vs. Activity

# Boxplot

- Graph-> Boxplots



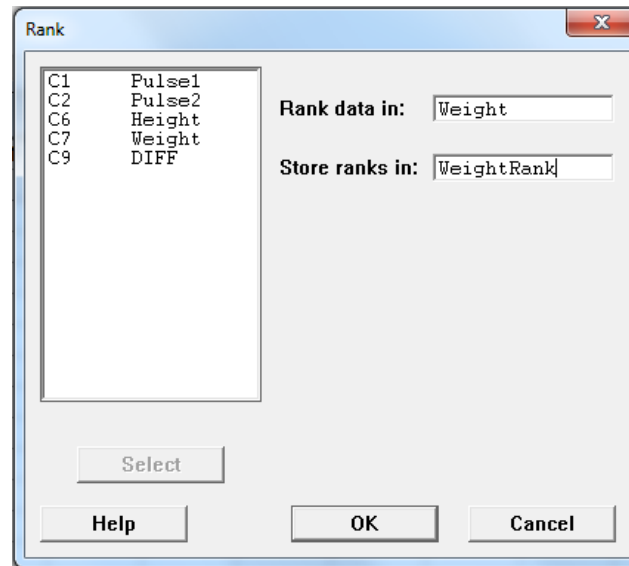
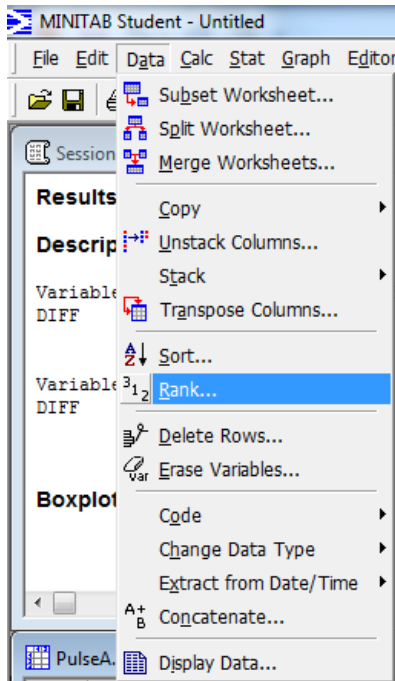
When the mouse is over the plot, Q1 etc. will show up.  
The same to outliers.

# Percentile in a column of data

Data-> Rank

51<sup>st</sup> Percentile in 'Weight'= ?

Total # in 'Weight' is 92. The 51<sup>st</sup> percentile is the  $92 * 51\% = 46.92$ th number. Find a number in WeightRank close to 46.92, the answer is the according Weight.



→	C1	C2	C3-T	C4-T	C5-T	C6	C7	C8-T	C9	C10
	Pulse1	Pulse2	Ran	Smokes	Gender	Height	Weight	Activity	DIFF	WeightRank
1	64	88	Ran	NonSmoker	Male	66.00	140	Moderate	24	39.5
2	58	70	Ran	NonSmoker	Male	72.00	145	Moderate	12	45.0

# 2. Probability distribution

- Example: Problem 3 in Exam #1

— Problem 3

[A] Using MINITAB, evaluate the following:

a. For  $X \sim \text{Bin}(n=15, p=.45)$

$P[x = 7] =$  \_\_\_\_\_.

$P[x \leq 6] =$  \_\_\_\_\_.

$P[x > 5] =$  \_\_\_\_\_.

b. For  $X \sim \text{Normal}$  with  $\mu = 11, \sigma = 2.5$

$P[x < 8] =$  \_\_\_\_\_.

81<sup>st</sup> percentile = \_\_\_\_\_.

c. For  $Y \sim \text{Poisson}$ , with  $\lambda = 10$

$P[x > 8] =$  \_\_\_\_\_.

$P[x = 5] =$  \_\_\_\_\_.

d. For  $X \sim \text{exponential}$ , with  $\lambda = 5$

Mean = \_\_\_\_\_.

Median = \_\_\_\_\_.

# Probability distribution

- Discrete
  - Binomial
  - Poisson
- Continuous
  - Normal
  - Exponential
  - Gamma

# Binomial

a. For  $X \sim \text{Bin}(n=15, p=.45)$

$P[X = 7] =$  \_\_\_\_\_

$P[X \leq 6] =$  \_\_\_\_\_

$P[X > 5] = 1 - P[X \leq 5] =$  \_\_\_\_\_

	C2	C3-T	C4-T
	Pulse2	Ran	Smokes
4	88	Ran	NonSmoke
8	70	Ran	NonSmoke
2	76	Ran	Smoke
5	78	Ran	Smoke
4	80	Ran	NonSmoke
4	84	Ran	NonSmoke
4	84	Ran	NonSmoke
8	72	Ran	NonSmoke
2	75	Ran	NonSmoke
5	118	Ran	NonSmoke
0	94	Ran	Smoke
0	96	Ran	NonSmoke

Binomial Distribution

- Probability
- Cumulative probability
- Inverse cumulative probability

Number of trials: 15  
Probability of success: .45

Input column: \_\_\_\_\_  
Optional storage: \_\_\_\_\_

Input constant: 7  
Optional storage: \_\_\_\_\_

Select Help OK Cancel

Binomial with  $n = 15$  and  $p = 0.45$

$x \quad P(X = x)$   
7     0.201344

Binomial Distribution

- Probability
- Cumulative probability
- Inverse cumulative probability

Number of trials: 15  
Probability of success: .45

Input column: \_\_\_\_\_  
Optional storage: \_\_\_\_\_

Input constant: 6  
Optional storage: \_\_\_\_\_

Select Help OK Cancel

Binomial with  $n = 15$  and  $p = 0.45$

$x \quad P(X \leq x)$   
6     0.452160

Binomial Distribution

- Probability
- Cumulative probability
- Inverse cumulative probability

Number of trials: 15  
Probability of success: .45

Input column: \_\_\_\_\_  
Optional storage: \_\_\_\_\_

Input constant: 5  
Optional storage: \_\_\_\_\_

Select Help OK Cancel

Binomial with  $n = 15$  and  $p = 0.45$

$x \quad P(X \leq x)$   
5     0.260760

$1 - 0.260760 = 0.73924$

# Poisson

c. For  $Y \sim \text{Poisson}$ , with  $\lambda = 10$

$$P[X > 8] = 1 - P[X \leq 8]$$

$$P[X = 5] =$$

Calc Stat Graph Editor Tools Window Help

- Calculator...
- Column Statistics...
- Rgw Statistics...
- Standardize...
- Make Patterned Data
- Make Indicator Variables...
- Set Base...
- Random Data
- Probability Distributions**
  - Chi-Square...
  - Normal...
  - F...
  - t...
  - Uniform...
  - Binomial...
  - Hypergeometric...
  - Discrete...
  - Integer...
  - Poisson...**
  - Beta...
  - Cauchy...
  - Exponential...
  - Gamma...
  - Laplace...
  - Largest Extreme Value...
  - Logistic...
  - Loglogistic...
  - Lognormal...
  - Smallest Extreme Value...
  - Triangular...
  - Weibull...
- Matrices

**Distribution Function**

h n = 15 and p = 0.45

	C2	C3-T	C4-T
	Pulse2	Ran	Smokes
4	88	Ran	NonSmoke
8	70	Ran	NonSmoke
2	76	Ran	Smoke
6	78	Ran	Smoke
4	80	Ran	NonSmoke
4	84	Ran	NonSmoke
4	84	Ran	NonSmoke
8	72	Ran	NonSmoke
2	75	Ran	NonSmoke
6	118	Ran	NonSmoke
0	94	Ran	Smoke
0	96	Ran	NonSmoke
2	84	Ran	Smoke

Poisson Distribution

Probability

Cumulative probability

Inverse cumulative probability

Mean: 10

Input column: \_\_\_\_\_

Optional storage: \_\_\_\_\_

Input constant: 8

Optional storage: \_\_\_\_\_

Select

Help OK Cancel

Poisson with mean = 10

x	P( X ≤ x )
8	0.332820

$$1 - 0.332820 = 0.66717$$

Poisson Distribution

Probability

Cumulative probability

Inverse cumulative probability

Mean: 10

Input column: \_\_\_\_\_

Optional storage: \_\_\_\_\_

Input constant: 5

Optional storage: \_\_\_\_\_

Select

Help OK Cancel

Poisson with mean = 10

x	P( X = x )
5	0.0378333



# Normal

b. For  $X \sim \text{Normal}$  with  $\mu = 11, \sigma = 2.5$

$P[X < 8] =$  \_\_\_\_\_

81<sup>st</sup> percentile = \_\_\_\_\_

Calc Stat Graph Editor Tools Window Help

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- Random Data
- Probability Distributions**
  - Chi-Square...
  - Normal...**
  - E...
  - F...
  - Uniform...
- Matrices

C2	C3-T	C4-T
Pulse2	Ran	Smokes
88	Ran	NonSmoke
70	Ran	NonSmoke
76	Ran	Smoke
78	Ran	Smoke
80	Ran	NonSmoke
84	Ran	NonSmoke
84	Ran	NonSmoke
72	Ran	NonSmoke
75	Ran	NonSmoke
118	Ran	NonSmoke
94	Ran	Smoke
96	Ran	NonSmoke
84	Ran	Smoke

Normal Distribution

Probability density  
 Cumulative probability  
 Inverse cumulative probability

Mean: 11  
 Standard deviation: 2.5

Input column:  
 Optional storage:  
 Input constant: 8  
 Optional storage:

Select Help OK Cancel

Normal with mean = 11 and standard deviation = 2.5

```

x  P( X <= x )
8  0.115070
    
```

Normal Distribution

Probability density  
 Cumulative probability  
 Inverse cumulative probability

Mean: 11  
 Standard deviation: 2.5

Input column:  
 Optional storage:  
 Input constant: .81  
 Optional storage:

Select Help OK Cancel

Normal with mean = 11 and standard deviation = 2.5

```

P( X <= x )      x
0.81  13.1947
    
```

# Exponential

d. For  $X \sim \text{exponential}$ , with  $\lambda = 5$

Mean = 1/5 = 0.2

Median = \_\_\_\_\_

Calc Stat Graph Editor Tools Window Help

- Calculator...
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  - Chi-Square...
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  - Beta...
  - Cauchy...
  - Exponential...**
  - Gamma...
  - Laplace...
  - Largest Extreme Value...
  - Logistic...
  - Loglogistic...
  - Lognormal...
  - Smallest Extreme Value...
  - Triangular...
  - Weibull...
- Matrices

pn = 2.5

x  
13.1947

	C2	C3-T	C4-T
	Pulse2	Ran	Smokes
1	88	Ran	NonSmoke
3	70	Ran	NonSmoke
2	76	Ran	Smoke
5	78	Ran	Smoke
4	80	Ran	NonSmoke
4	84	Ran	NonSmoke
4	84	Ran	NonSmoke
3	72	Ran	NonSmoke
2	75	Ran	NonSmoke
5	118	Ran	NonSmoke
0	94	Ran	Smoke
0	96	Ran	NonSmoke
5	84	Ran	NonSmoke

Exponential Distribution

Probability density  
 Cumulative probability  
 Inverse cumulative probability

Scale:  [= Mean when Threshold = 0]

Threshold:

Input column: \_\_\_\_\_  
 Optional storage: \_\_\_\_\_

Input constant:   
 Optional storage: \_\_\_\_\_

Select Help OK Cancel

Exponential with mean = 0.2

$P(X \leq x)$                        $x$   
 0.5    0.138629

# 3. Random data, column statistics, row statistics, monte carlo

- For example Prob. 3 in Exam 2

[A] The lifetime of three lamps is exponentially distributed with means 120, 160 and 130 hours respectively. If they are placed in parallel in a system, estimate (using Monte Carlo simulation with 500 iterations), the

(a)  $\text{Prob}[\text{system lifetime} > 150] = \underline{\hspace{2cm}}$ .

(b) Is the probability distribution of system lifetime

Normal?                   .

Exponential?                   .

Gamma?                   .

How do you check this? Give p values.

[B] The acceleration  $g$  due to gravity is measured by dropping an object and measuring the time  $t$  it takes to travel a distance  $S$ . Assuming  $s$  and  $t$  are normally distributed with means and uncertainties as indicated:

$$s = 2.2 \pm 0.01m$$

$$t = 0.67 \pm 0.015s$$

(i) Estimate (using Monte Carlo simulation with 500 iterations),  $g$  and its uncertainty.

$g = \underline{\hspace{2cm}} \pm \underline{\hspace{2cm}}$  [Hint:  $s = \frac{1}{2}gt^2$ ]

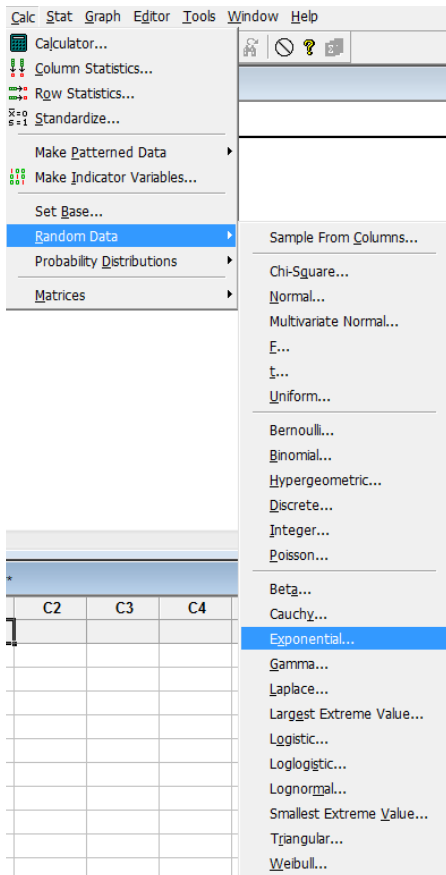
(ii) Run an Exec file (100 iterations) on the mean value of  $g$ . Find the average.

Copy the exec file.

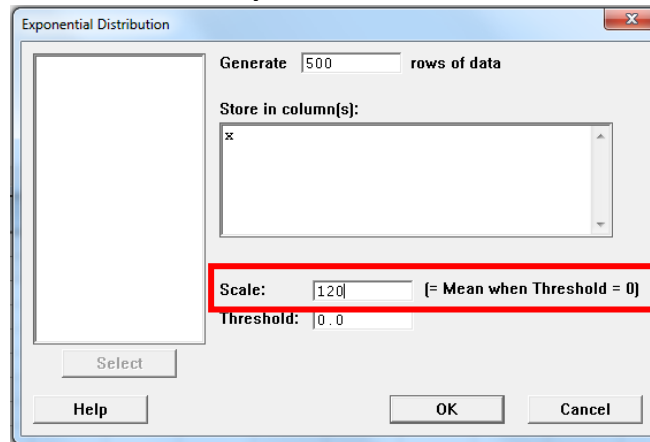
# Random data

[A] The lifetime of three lamps is exponentially distributed with means 120, 160 and 130 hours respectively. If they are placed in parallel in a system, estimate (using Monte Carlo simulation with 500 iterations), the

(a)  $\text{Prob}[\text{system lifetime} > 150] = \underline{\hspace{2cm}}$ .



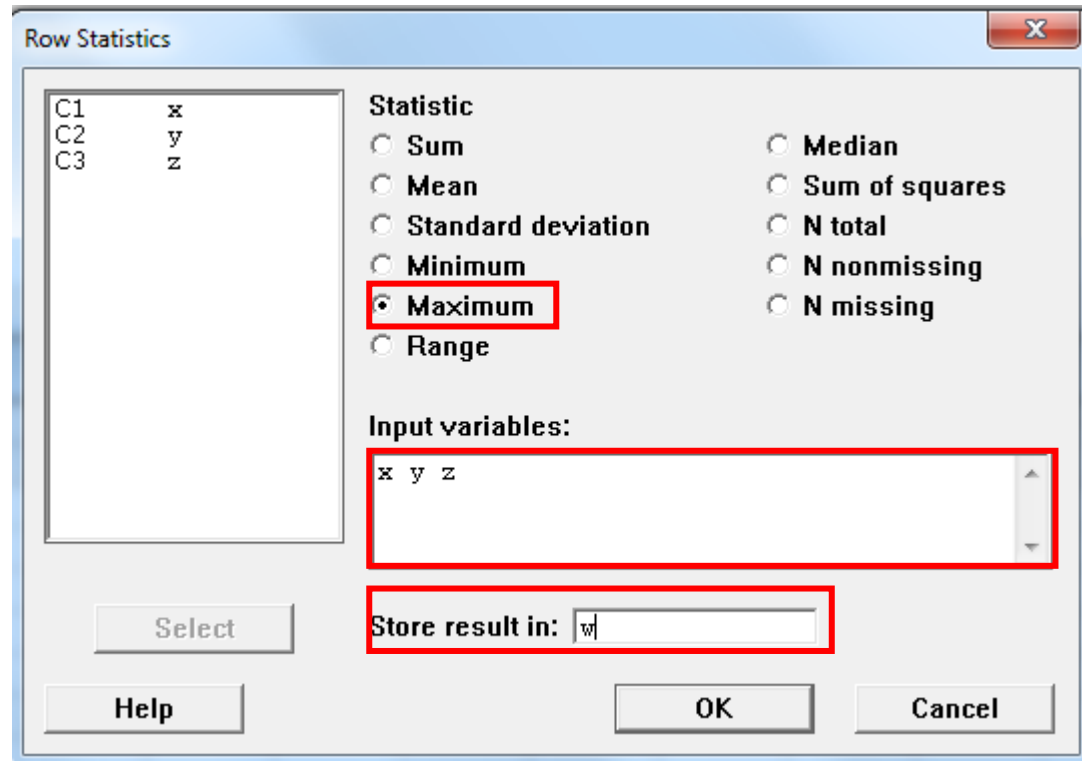
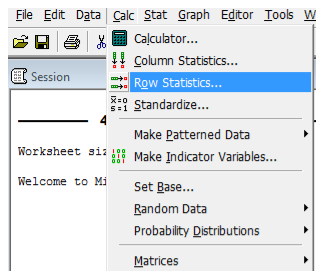
Generate x,y,z columns of data



C1	C2	C3
x	y	z
198.169	68.984	94.73
188.082	1.885	77.73
15.990	279.901	132.09
265.590	21.292	135.30
227.518	126.934	86.40
256.802	285.487	27.64
138.813	17.422	163.50
103.351	62.350	14.05
236.884	75.233	37.44
112.131	19.700	161.52
166.417	50.774	52.12

# Row statistics

Calc-> Row Statistics

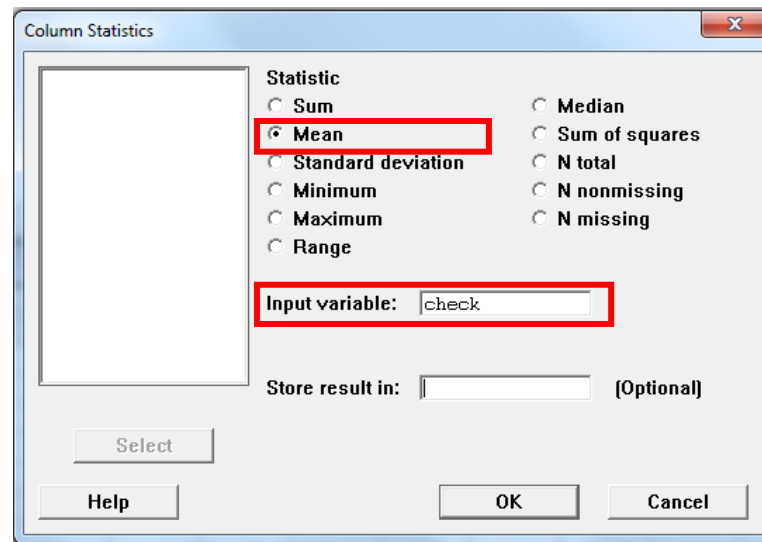
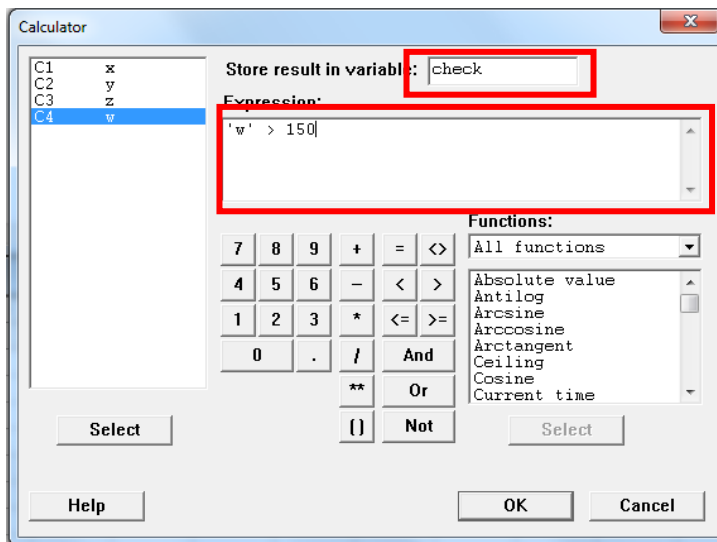


x	y	z	w
198.169	68.984	94.73	198.17
188.082	1.885	77.73	188.08
15.990	279.901	132.09	279.90
265.590	21.292	135.30	265.59
227.518	126.934	86.40	227.52
256.802	285.487	27.64	285.49
138.813	17.422	163.50	163.50
102.351	62.350	14.05	102.35

# Column statistics

[A] The lifetime of three lamps is exponentially distributed with means 120, 160 and 130 hours respectively. If they are placed in parallel in a system, estimate (using Monte Carlo simulation with 500 iterations), the

(a)  $\text{Prob}[\text{system lifetime} > 150] =$  \_\_\_\_\_.



**Mean of check**

Mean of check = 0.7

# Monte Carlo

[B] The acceleration  $g$  due to gravity is measured by dropping an object and measuring the time  $t$  it takes to travel a distance  $s$ . Assuming  $s$  and  $t$  are normally distributed with means and uncertainties as indicated:

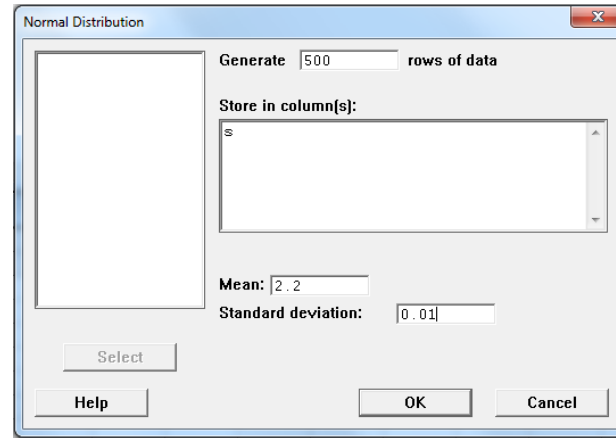
$$s = 2.2 \pm 0.01m$$

$$t = 0.67 \pm 0.015s$$

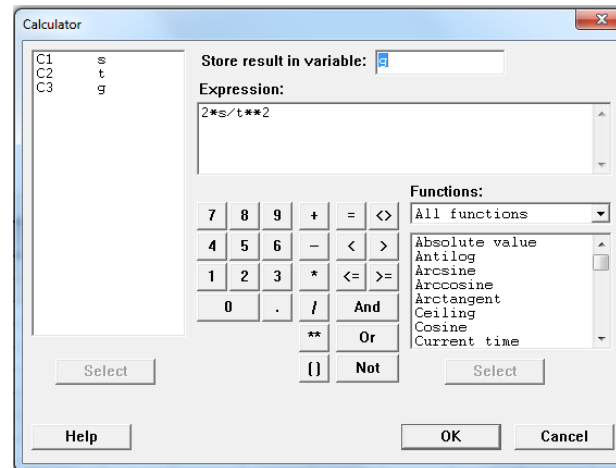
(i) Estimate (using Monte Carlo simulation with 500 iterations),  $g$  and its uncertainty.

$$g = \text{_____} \pm \text{_____} \quad [\text{Hint: } s = \frac{1}{2}gt^2]$$

## 1. Generate 2 columns for 's' and 't'

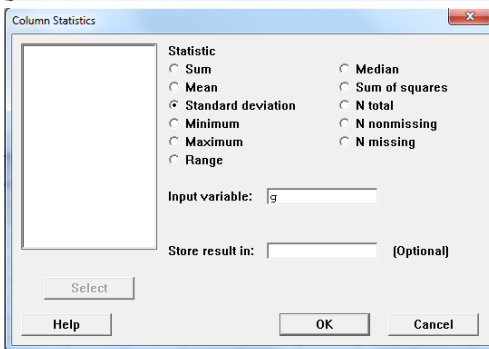
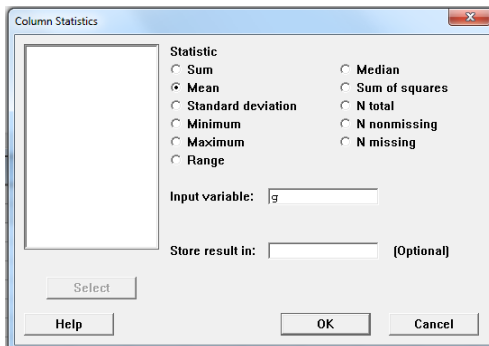


## 2. Calculate 'g'



s	t	g
2.19751	0.666008	9.9084
2.19201	0.665263	9.9057
2.20787	0.691967	9.2222
2.21312	0.670899	9.8338
2.21404	0.677959	9.6340
2.20907	0.692054	9.2248
2.19018	0.669479	9.7732
2.20587	0.670413	9.8158
2.20045	0.681206	9.4706

## 3. Column statistic for 'g'



**Mean of g**

Mean of g = 9.86910

**Standard Deviation of g**

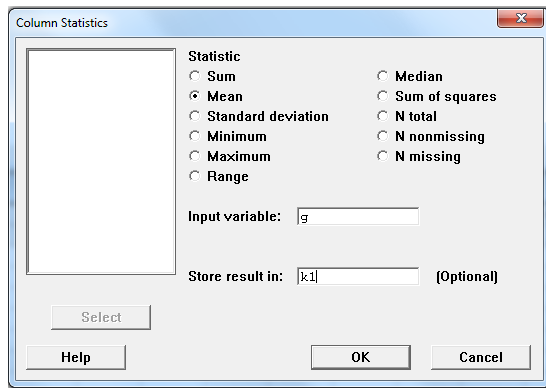
Standard deviation of g = 0.469206

# Monte Carlo

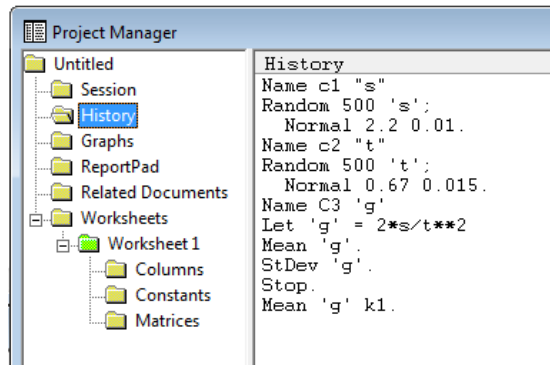
(ii) Run an Exec file (100 iterations) on the mean value of g. Find the average.

Copy the exec file.

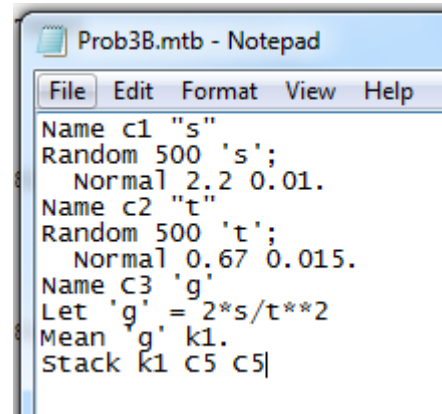
## 1. Store mean of 'g' in k1



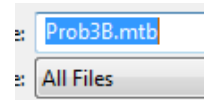
## 2. Project manager -> History-> Copy all the scribe



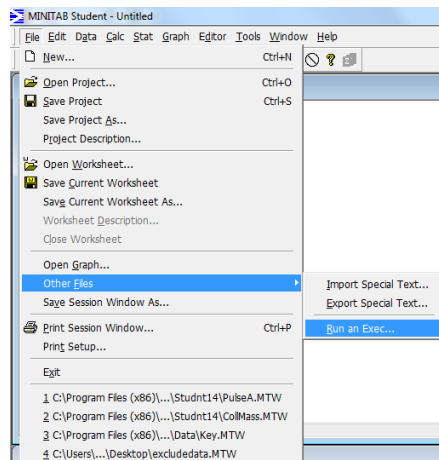
## 3. Tools-> Notepad-> paste sctibe-> add 'stack k1 C5 C5'



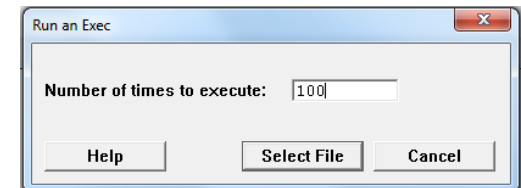
## 4. Save as 'Prob3B.mtb'. Choose 'All Files'



## 5. File->Other Files->Run an Exec



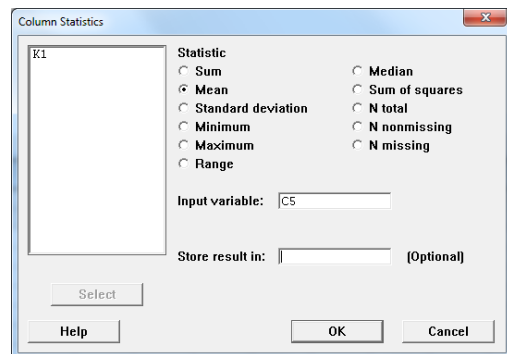
## 6. Indicate trails number and select 'Prob3B.mtb'





# Monte Carlo

- After running the exec file, calculate the mean of C5



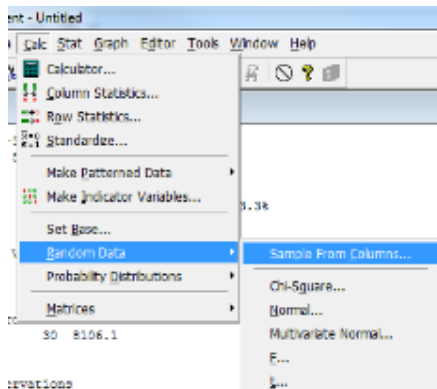
## Mean of C5

Mean of C5 = 9.81614

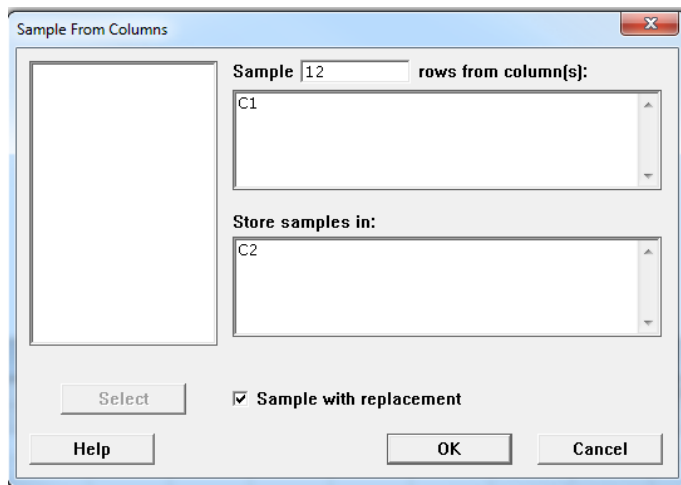
# Another way to generate data - bootstrap

- Prob 6 in Exam 2

1. Calc-> Random data-> Sample from column



2. Input sample number, input column and output column



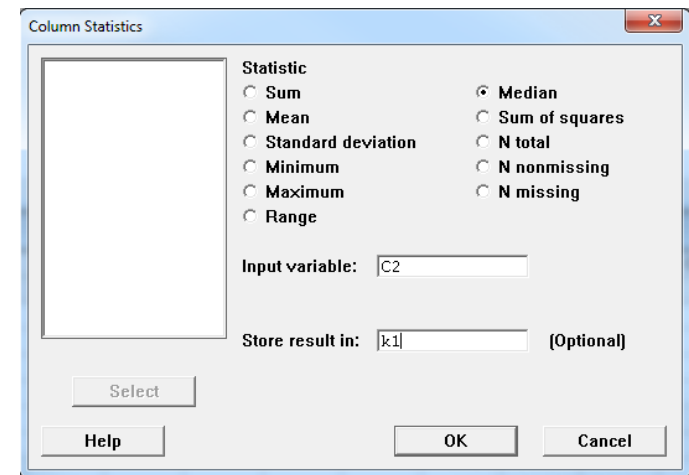
[A] Following sample is taken from an unknown population:

$\{x_i\}$ : 10, 19, 22, 13, 9, 16, 12, 24, 17, 23, 18, 14

Using an appropriate approach, obtain an estimate of the standard error of the median,  $\sigma_{\tilde{x}}$ .

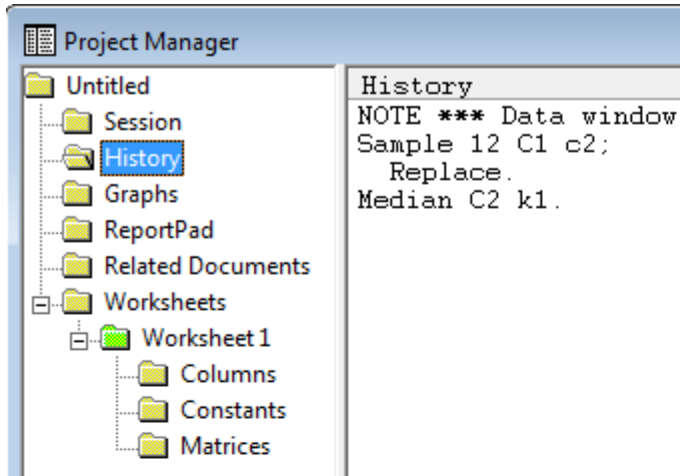
C1	C2
10	9
19	9
22	18
13	9
9	23
16	24
12	17
24	9
17	12
23	23
18	19
14	18

3. Calc -> column statistics-> Median-> Input variable C2 store k1

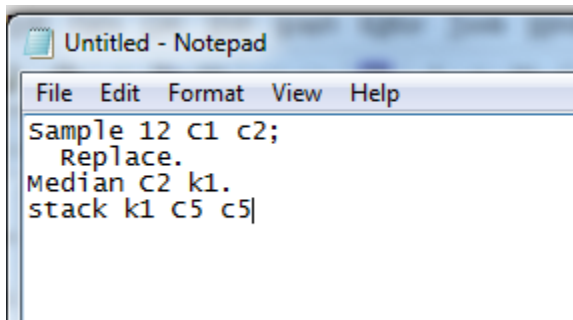


# Bootstrap

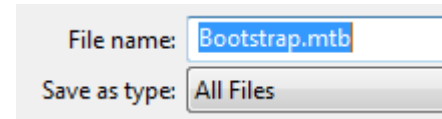
4. Project Manager-> History-> Copy



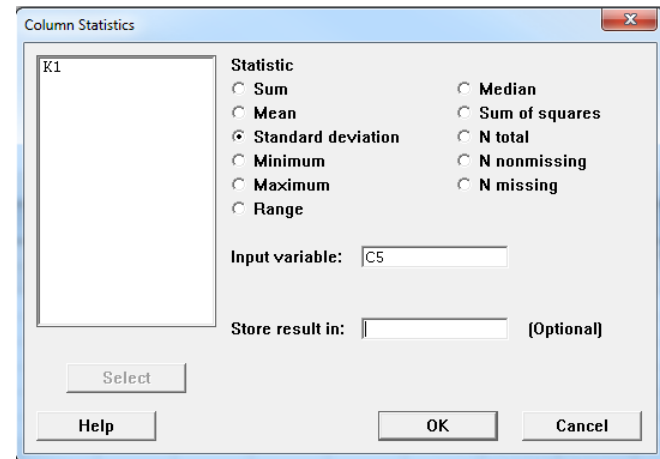
5. Paste it in Notepad and add 'stack k1 C5 C5'



6. Save as 'Bootstap.mtb'



7. Run the exec file 100 times, then Column statistics-> Standard deviation -> Input C5



**Standard Deviation of C5**

Standard deviation of C5 = 1.97215

# 4. t-test, z-test, power analysis, probability plot

- Problem 2 in Exam 2

We want to test if there is a difference in true average bacteria count (number of colonies/ $ft^3$ ) between carpeted ( $X_i$ ) and uncarpeted ( $Y_i$ ) rooms. The following samples were taken in a hospital: [Assume Equal Variance 5]

$X_i$	15.3	16.4	16.2	15.5	15.0	15.3	14.4	15.1	15.6	15.2	16.3
$Y_i$	13.4	14.8	13.0	14.1	13.7	15.4	16.3	13.2	14.3	15.3	13.9

[Note:  $\sum x_i = 170.3$ ;  $\sum y_i = 157.4$ ]

(a) State appropriate hypothesis to be tested:

(b) What type of test would you use?

(c) Give values of

Test statistic =

P-value =

s.d. =

(d) Is  $H_0$  rejected or not @  $\alpha = .05$  ?

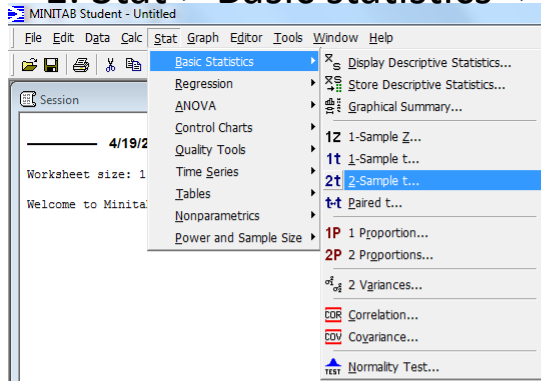
(e) Give a 95% CI on  $\mu_x - \mu_y$ :

(f) If actually  $\mu_x - \mu_y = 1$ , how large a sample size would be necessary to test the difference, with a power of .95? (Take  $\alpha = .05$  )

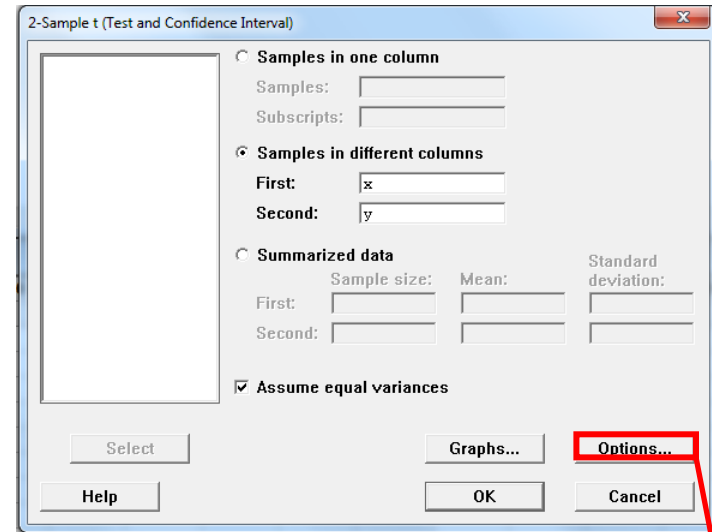
(g) What main assumption underlies your test? Is the assumption 'justified'?

# T-test, z-test

## 1. Stat-> Basic statistics -> 2-sample t



## 2. Input samples in different columns



## 3. Options-> Confidence level, test difference, Alternative

Two-sample T for x vs y

	N	Mean	StDev	SE Mean
x	11	15.482	0.611	0.18
y	11	14.31	1.04	0.31

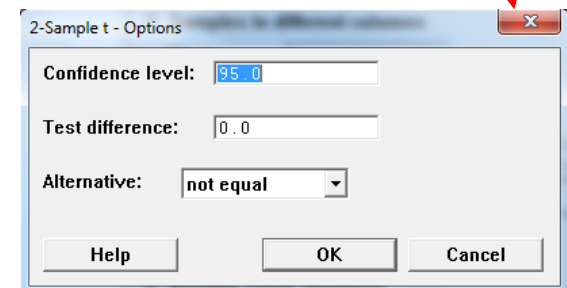
Difference =  $\mu(x) - \mu(y)$

Estimate for difference: 1.17273

95% CI for difference: (0.41628, 1.92917)

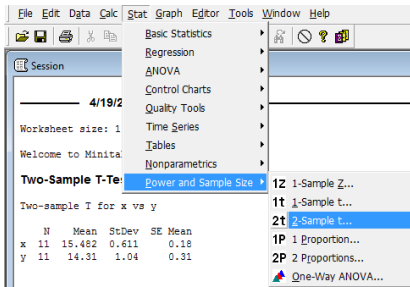
T-Test of difference = 0 (vs not =): T-Value = 3.23 P-Value = 0.004 DF = 20

Both use Pooled StDev = 0.8505

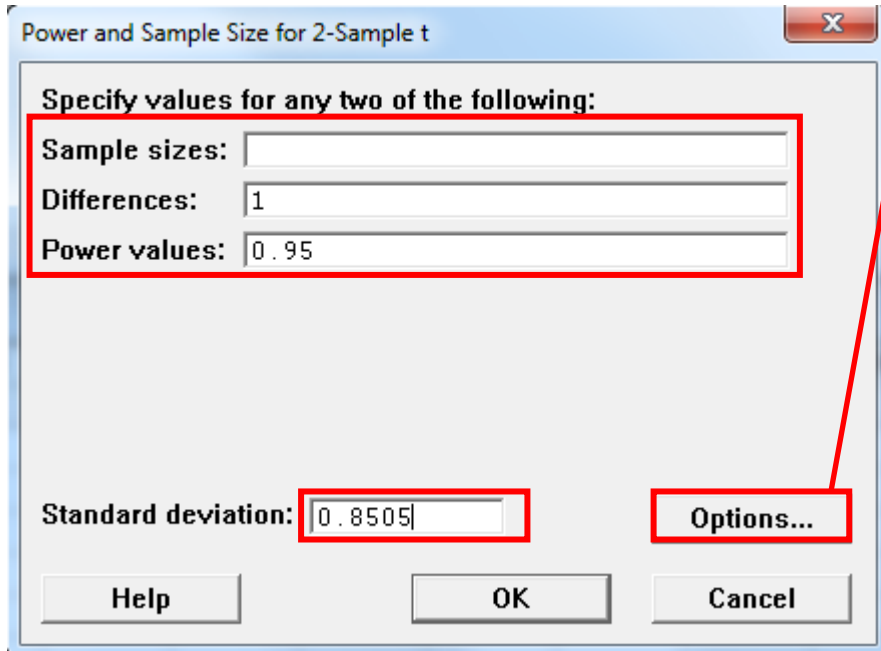


# Power analysis

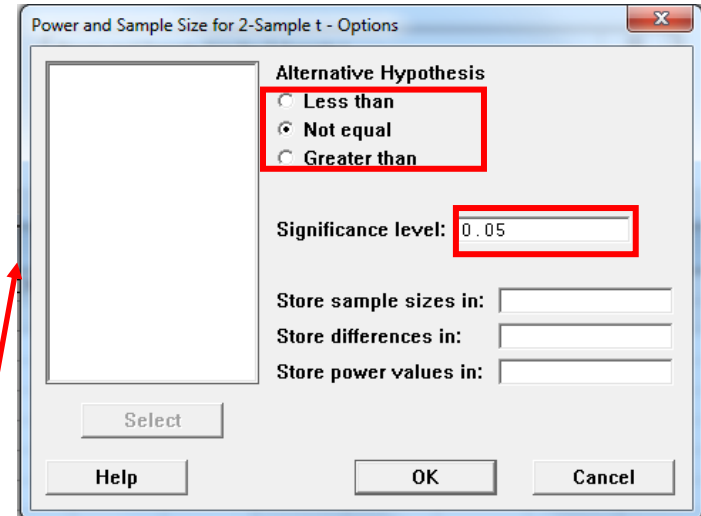
1. Stat-> Power analysis -> 2 sample t test



2. Input differences and power values, and s.d.



3. Alternative Hypothesis and sig. level



2-Sample t Test

Testing mean 1 = mean 2 (versus not =)  
 Calculating power for mean 1 = mean 2 + difference  
 Alpha = 0.05 Assumed standard deviation = 0.8505

Difference	Sample Size	Target Power	Actual Power
1	20	0.95	0.951810

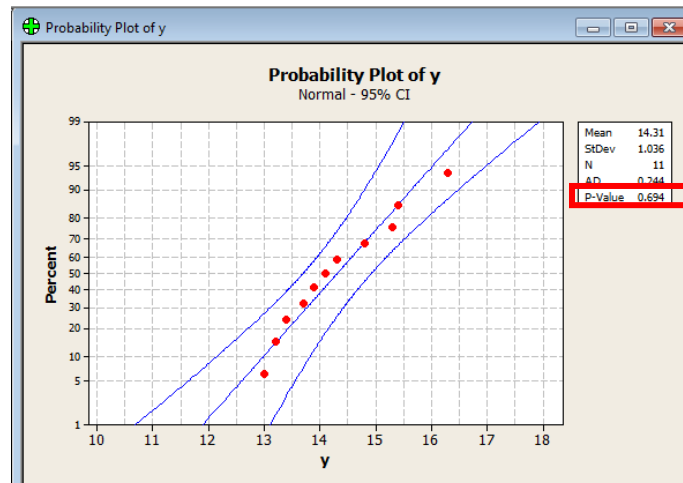
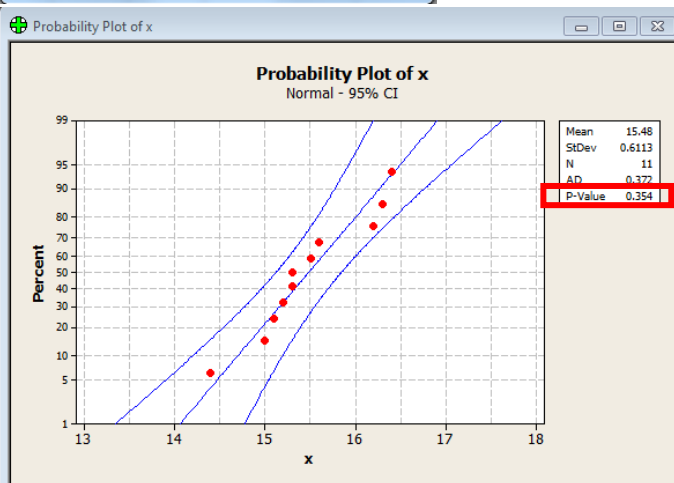
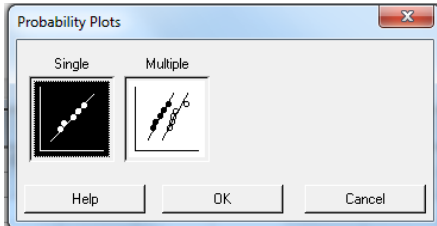
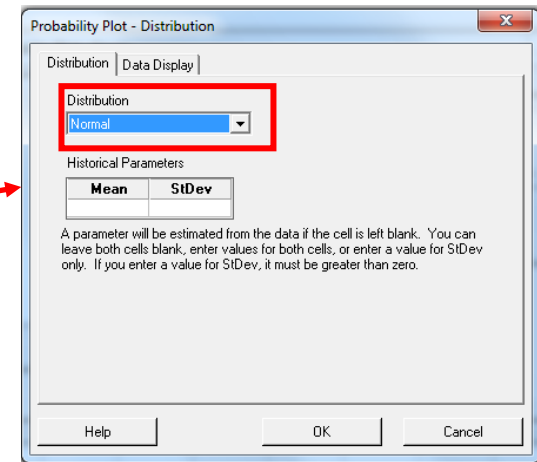
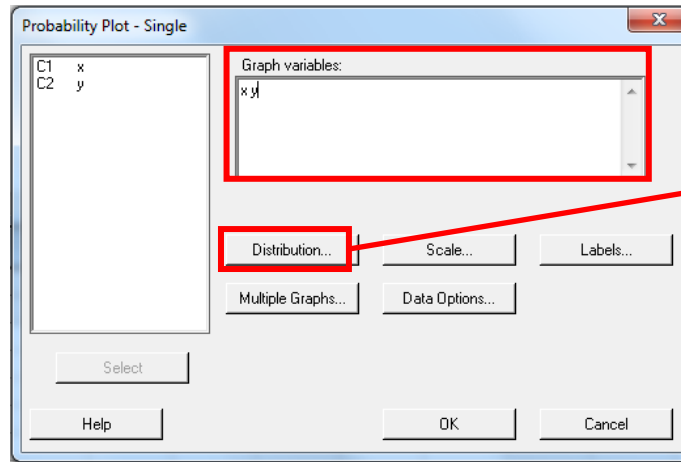
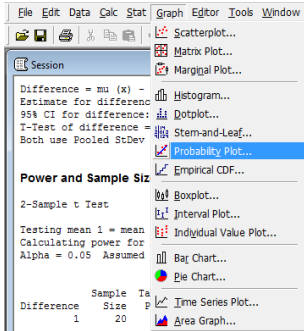
The sample size is for each group.

# Probability plot

Graph-> Probability Plot

Choose the probability distribution we want to test

Insert variables



If p-value > 0.05, it is normal at 95% confidence, otherwise, it is not.

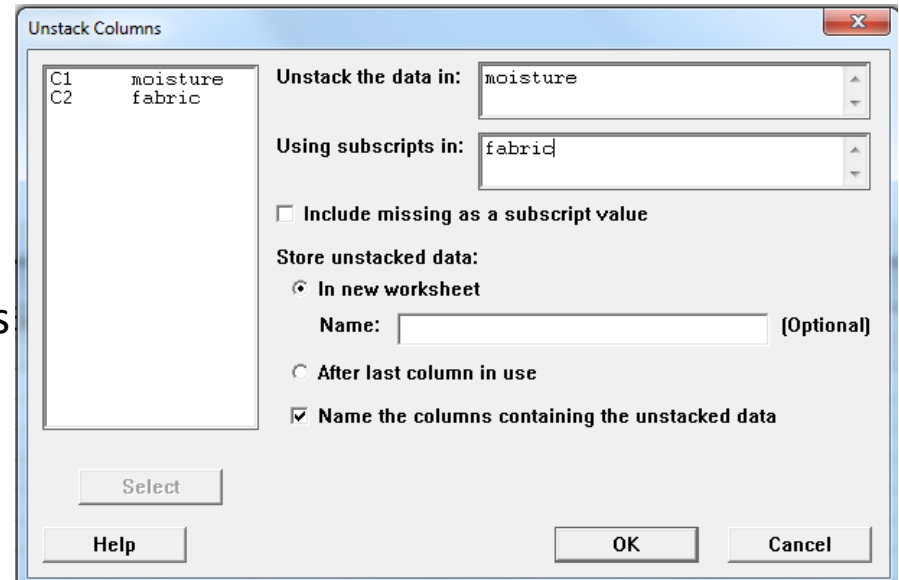
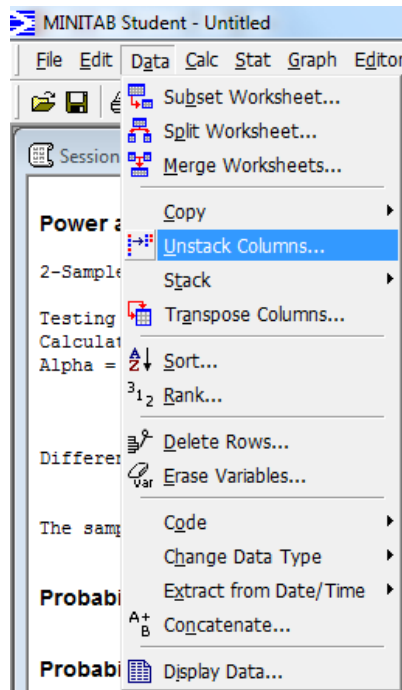
# 5. Control charts

- Devore datasets
- Ex16-08

## 2. Input data and subscripts

### 1. Data-> Unstack Columns

C1	C2-T
moisture	fabric
12.19999	#1
12.4	#1
12.9	#1
13.2	#1
12.8	#1
13.9	#1
12.2	#1
12.6	#1
14.6	#1
12.8	#1
12.6	#1
13.5	#1
13.4	#1

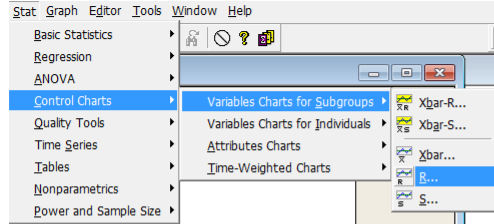
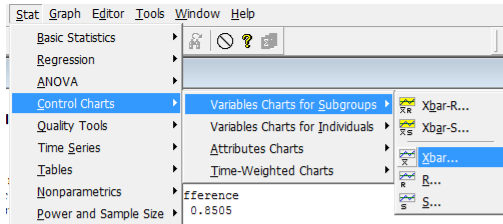


	C1	C2	C3	C4	C5
	moisture_1	moisture_2	moisture_3	moisture_4	moisture_5
1	12.2000	12.1000	13.3000	13.0000	13.0000
2	12.4000	13.3000	12.8000	12.6000	12.9000
3	12.9000	12.7000	14.2000	12.5000	12.9000
4	13.2000	13.0000	13.0000	12.6000	13.9000
5	12.8000	12.3000	12.2000	13.3000	12.0000
6	13.9000	13.4000	13.1000	12.4000	13.2000
7	12.2000	14.4000	12.4000	12.4000	12.5000
8	12.6000	12.8000	13.5000	13.9000	13.1000
9	14.6000	13.4000	12.2000	13.7000	12.5000
10	12.8000	12.3000	12.6000	13.2000	12.8000
11	12.6000	13.1000	12.7000	13.2000	12.3000
12	13.5000	12.3000	12.8000	13.1000	12.9000
13	13.4000	13.3000	12.0000	12.9000	13.1000
14	13.5000	12.4000	13.0000	13.6000	13.4000
15	12.3000	12.8000	13.0000	12.8000	13.5000
16	12.6000	13.4000	12.1000	13.2000	13.3000

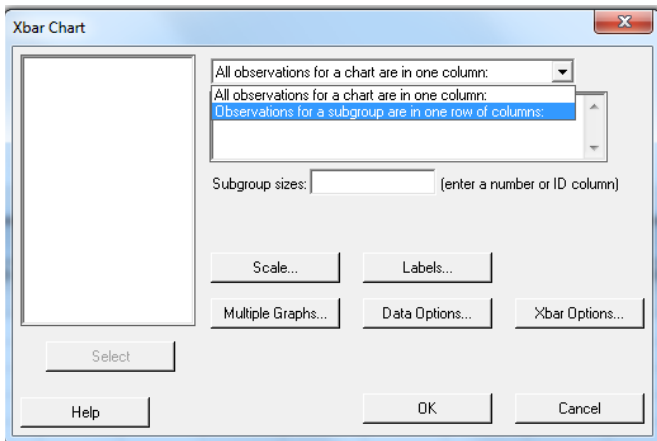


# Control Chart

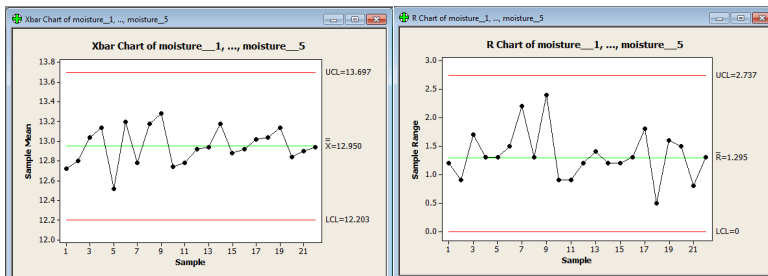
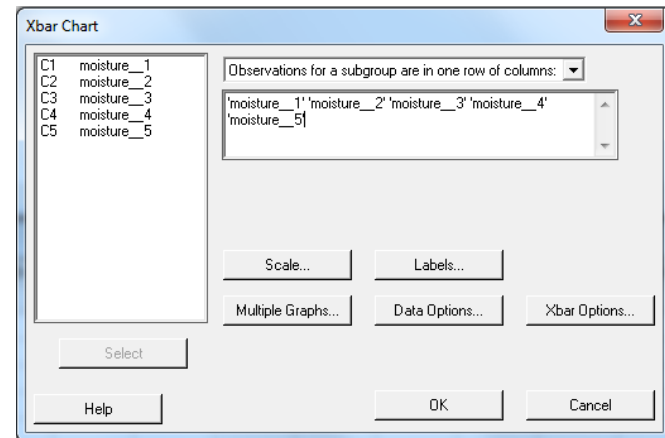
Stat-> Control Charts-> Variables charts for subgroups->Xbar/R



Choose 'Observations for a subgroup are in one row of columns'



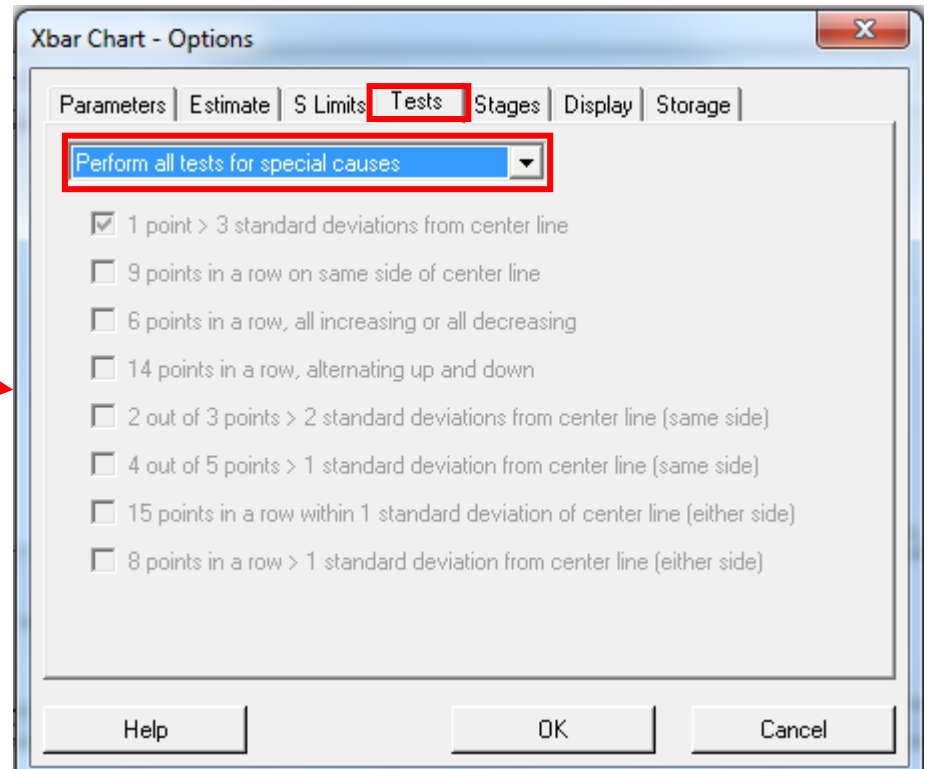
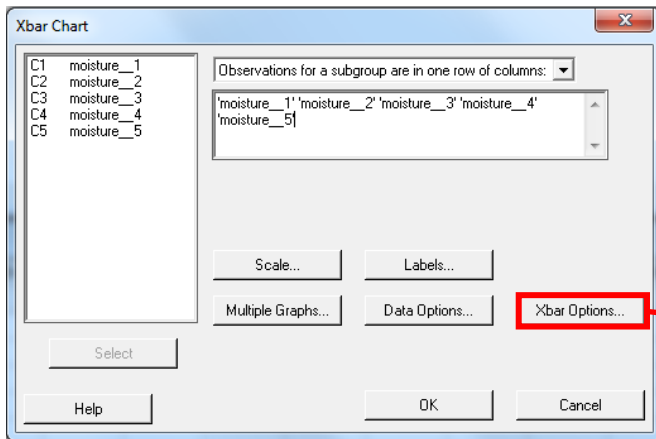
Input all the columns



# Control chart

- Perform eight tests:  
Choose Xbar Options

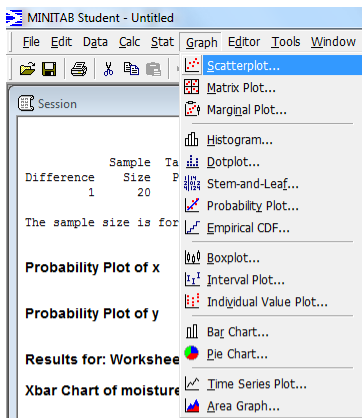
Test-> 'Perform all tests for special causes'



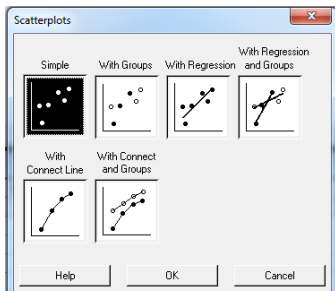
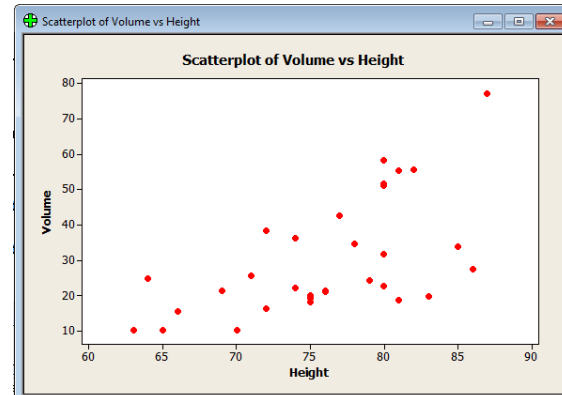
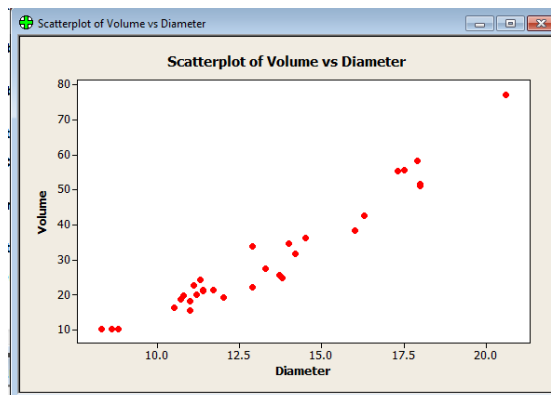
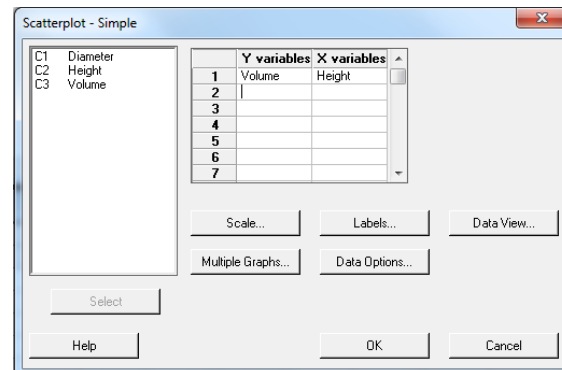
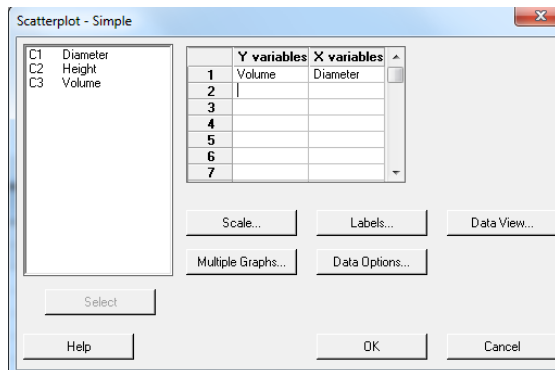
# 6. Scatter plot, regression

- MINITAB worksheet TREES
- (a) Obtain the scatter plot of the data(volume vs. diameter and volume vs. height)

Graph-> Scatterplot



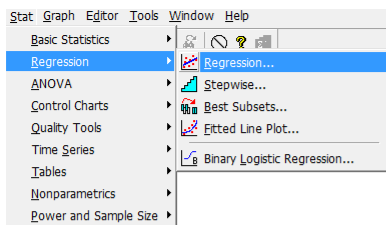
Input Y and X:



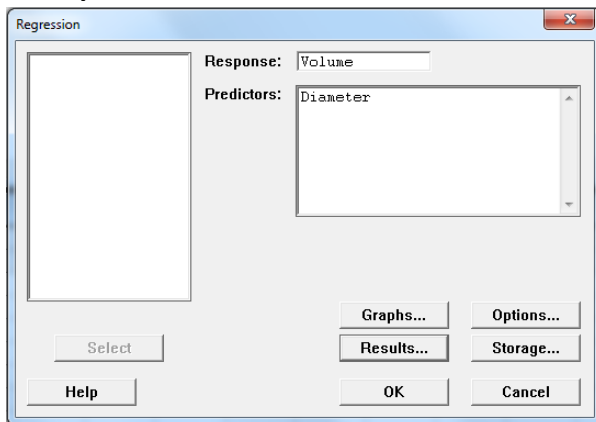
# Regression

- (b) Use diameter as a predictor of volume, do a least square analysis and obtain simple linear parameter

Stat-> Regression-> Regression



Input Volume and Diameter



## Regression Analysis: Volume versus Diameter

The regression equation is  
 Volume = - 36.9 + 5.07 Diameter

Predictor	Coef	SE Coef	T	P
Constant	-36.943	3.365	-10.98	0.000
Diameter	5.0659	0.2474	20.48	0.000

S = 4.25199    R-Sq = 93.5%    R-Sq(adj) = 93.3%

## Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	7581.8	7581.8	419.36	0.000
Residual Error	29	524.3	18.1		
Total	30	8106.1			

## Unusual Observations

Obs	Diameter	Volume	Fit	SE Fit	Residual	St Resid
31	20.6	77.000	67.413	1.972	9.587	2.55RX

R denotes an observation with a large standardized residual.  
 X denotes an observation whose X value gives it large influence.